



# Enthalpies of formation of methyl substituted naphthalenes

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## ABSTRACT

In this work, the enthalpies of formation for the homologous series of methyl substituted naphthalene isomers were calculated using the AM1, PM3, B3PW91, and G3MP2 methods. This work was done primarily to address the lack of data available for many of these compounds and to find the most cost-effective method to calculate the enthalpy of formation. In addition, we explored the development of a group-additivity model as a fast method to calculate the enthalpy of formation. Using this model, two sets of interaction parameters were derived. One set from the G3MP2 results and the other from the B3PW91 results. These parameters differ by an average of 2.3 kJ mol<sup>-1</sup>, implying that the simpler B3PW91 calculations may be used to develop a group-additivity model. The model using the G3MP2 derived parameters deviate from the experimental values with a RMS of 3.0 kJ mol<sup>-1</sup>. Using the B3PW91 parameters, the model has an RMS of 9.1 kJ mol<sup>-1</sup>.

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## 1. Introduction

Compilations of basic physical property data exist for thousands of compounds [1–3]; however, it is infeasible, for many reasons, including cost, manpower, and experimental difficulty, to measure the properties of every existing and newly created compound. In response to these limitations, and to increase the understanding of the underlying chemistry, multiple calculation and estimation methods have been developed to predict the physical properties of compounds. The enthalpy of formation is one of these basic properties and describes the amount of energy contained in a molecule. Knowing the enthalpy of formation allows a chemist to determine many other molecular properties, including reactivity and the reduction–oxidation potential [4,5].

In this work, the standard enthalpies of formation ( $\Delta H_f^\circ_{298}$ ) for all eighty-nine members of the homologous series of methyl substituted benzene and naphthalene isomers have been calculated using semi-empirical and *ab initio* methods. We have evaluated these methods for their accuracy, speed, and ease of calculation. The prime motivation for this work was to address the lack of data available for the methyl substituted naphthalenes. Of the seventy-six naphthalene compounds, only seven have had their enthalpies of formation experimentally measured and thirty-four have no physical property measurements reported in the literature [1–3]. A secondary driver for this work was to explore the development of a group-additivity model for aromatic compounds.

Group-additivity models, first developed by Benson, are fast, back-of-the envelope calculations that perform well for many series of compounds [6]. Their main drawback is that to develop these models, each group must be defined and the interactions between groups must be quantified. Previously, Whiteside and Carreira attempted to improve Benson's group additivity method for predicting the enthalpy of formation of hydrocarbons and extend it to include aromatic compounds [5,6]. This predictive work was successful for the compounds studied; however, verifying it as a general technique was difficult due to the lack of experimental measurements with which to compare the results. Also, since the group additivity parameters are based on experimental data, the interaction parameters cannot be determined for classes of compounds lacking this data. As a solution to this lack of data, we have performed calculations, whose results were used to extend the group additivity parameters and to predict the  $\Delta H_f^\circ_{298}$  of methyl substituted naphthalenes and benzenes.

## 2. Theory

The Gaussian 03 software package [7] was used to calculate the  $\Delta H_f^\circ_{298}$  using the AM1 [8], PM3 [9,10], B3PW91 6-31++G(d,p) [11,12], and G3MP2 methods [13]. The semi-empirical AM1 and PM3 methods were used as baselines against which to compare the other methods. The B3PW91 and G3MP2 methods were used as they are the most rigorous computations of these compounds that we could perform on our system. We chose the B3PW91 DFT functional as it fulfills the uniform electron gas limit and shows improvement over B3LYP for predicting atomization energies and hydrocarbon bond dissociation energies [14,15]. Using the G3MP2

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**Table 1**  
Methyl substituted benzenes. Experimental and calculated  $\Delta H_f^{\circ 298}$  values in  $\text{kJ mol}^{-1}$ .

Name	CAS	Expt.	Reference	AM1	PM3	B3PW91 6-31++G(d,p)		G3MP2	
						iso <sup>a</sup>	homo <sup>b</sup>	iso <sup>a</sup>	homo <sup>b</sup>
Benzene	71-43-2	82.9 ± 0.0	3	91.7	97.8	82.9	82.9	82.9	82.9
1-Methylbenzene	108-88-3	50.1 ± 1.1	3	59.8	58.5	55.4	50.1	50.2	50.1
1,2-Dimethylbenzene	95-47-6	19.0 ± 1.1	3	30.5	22.6	29.8	19.3	16.8	16.5
1,3-Dimethylbenzene	108-38-3	17.2 ± 0.8	3	28.1	19.4	28.3	17.8	17.7	17.4
1,4-Dimethylbenzene	106-42-3	17.9 ± 1.0	3	27.8	19.3	26.1	15.5	18.3	18.0
1,2,3-Trimethylbenzene	526-73-8	-9.6 ± 1.3	3	4.3	-12.5	10.4	-5.4	-10.9	-11.3
1,2,4-Trimethylbenzene	95-63-6	-13.9 ± 1.1	3	-1.2	-16.4	0.5	-15.3	-15.3	-15.7
1,3,5-Trimethylbenzene	108-67-8	-15.9 ± 1.5	3	-3.5	-19.5	1.1	-14.7	-14.8	-15.2
1,2,3,4-Tetramethylbenzene	488-23-3	-37.6 ± 1.2	3	-21.8	-46.6	-8.6	-29.7	-38.2	-38.7
1,2,3,5-Tetramethylbenzene	527-53-7	-44.4 ± 1.2	3	-27.3	-51.4	-16.5	-37.5	-42.8	-43.3
1,2,4,5-Tetramethylbenzene	95-93-2	-47.1 ± 1.9	3	-30.4	-52.9	-22.1	-43.2	-48.3	-48.8
1,2,3,4,5-Pentamethylbenzene	700-12-9	-67.2 ± 2.2	3	-47.4	-83.1	-26.7	-53.0	-65.0	-65.6
1,2,3,4,5,6-Hexamethylbenzene	87-85-4	-77.4 ± 2.5	3	-61.9	-109.4	-26.7	-58.3	-77.6	-78.4

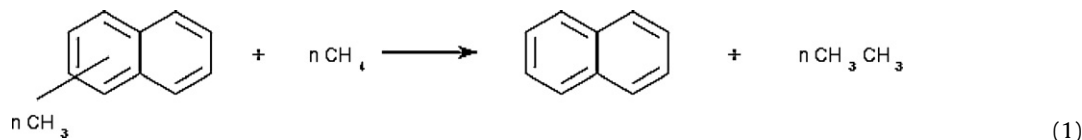
<sup>a</sup> These values calculated using the isodesmic equation, Eq. (3).

<sup>b</sup> These values calculated using the homodesmotic equation, Eq. (4).

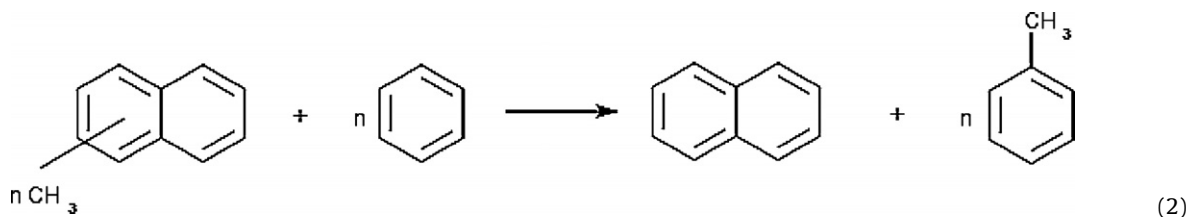
method, the largest compounds required a 64-bit operating system and used up to 3.3GB RAM, 96GB scratch space, and 30.3 hrs of CPU time on a 2.8 GHz AMD Opteron Processor.

We used isodesmic [16] and homodesmotic [17] reactions and calculations to determine the enthalpy of formation of these compounds when using the B3PW91 and G3MP2 methods; the AM1 and PM3 methods provide the enthalpy of formation directly. An isodesmic reaction has the same number and type of bonds

of carbon atom ( $sp^3$ ,  $sp^2$ ,  $sp$ ) with zero, one, two, and three hydrogens attached in the reactants and products [18]. These types of reactions result in values that are nearly size independent because correlation effects are canceled out and they make use of accurate experimental data [17–19]. Since the compounds studied are a homologous series, we were able to use the same reaction for each compound and simply alter the stoichiometric quantities ( $n$ ). The isodesmic reaction was of the form:



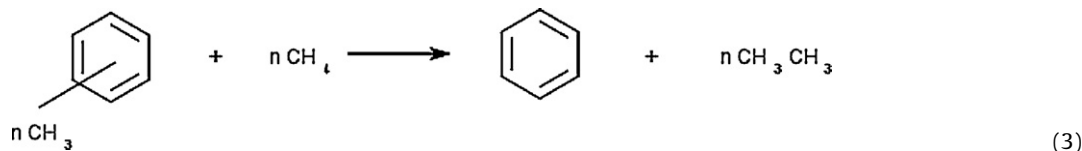
and the homodesmotic form of this reaction is:



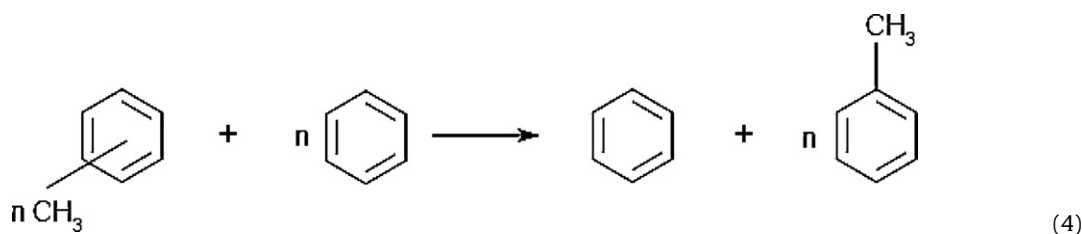
on each side of the equation. A homodesmotic reaction is an isodesmic reaction where there are equal numbers of each type of carbon-carbon bond ( $sp^3-sp^3$ ,  $sp^3-sp^2$ ,  $sp^3-sp$ , etc.) in the reactants and products and there are equal numbers of each type

The values of the enthalpies of formation used in these equations are: naphthalene  $150.6 \text{ kJ mol}^{-1}$ ; methane  $-74.6 \text{ kJ mol}^{-1}$ ; ethane  $-84.0 \text{ kJ mol}^{-1}$ ; toluene  $50.1 \text{ kJ mol}^{-1}$ ; and benzene  $82.9 \text{ kJ mol}^{-1}$  and were obtained from the NIST webbook [3].

We verified and validated this method by using the isodesmic equation:



and the homodesmotic equation:



**Table 2a**  
Methyl substituted naphthalenes. Experimental and calculated  $\Delta H_f^{\circ}$  values in  $\text{kJ mol}^{-1}$ .

Name	CAS	Expt.	Reference	AM1	PM3	B3PW91 6-31++G(d,p)		G3MP2	
						iso <sup>a</sup>	homo <sup>b</sup>	iso <sup>a</sup>	homo <sup>b</sup>
Naphthalene	91-20-3	150.6 ± 1.1	3	169.1	169.5	150.6	150.6	150.6	150.6
1-Methylnaphthalene	90-12-0	116.9 ± 2.7	3	141.3	135.7	126.4	121.7	117.8	117.7
2-Methylnaphthalene	91-57-6	116.1 ± 2.6	3	136.8	129.9	122.2	117.6	116.6	116.4
1,2-Dimethylnaphthalene	573-98-8			115.3	104.1	108.1	97.0	90.9	90.7
1,3-Dimethylnaphthalene	575-41-7			109.1	96.2	98.0	86.9	83.6	83.4
1,4-Dimethylnaphthalene	571-58-4			113.7	102.4	102.8	91.7	85.6	85.4
1,5-Dimethylnaphthalene	571-61-9			113.9	102.5	102.7	91.7	85.5	85.3
1,6-Dimethylnaphthalene	575-43-9			109.0	96.1	98.1	87.0	83.9	83.6
1,7-Dimethylnaphthalene	575-37-1			109.8	97.0	98.0	87.0	83.8	83.5
1,8-Dimethylnaphthalene	569-41-5	108.8 ± 3.0	3	133.4	115.7	130.4	119.3	111.0	110.7
2,3-Dimethylnaphthalene	581-40-8	79.9 ± 1.1	3	108.0	94.7	96.9	85.8	83.2	82.9
2,6-Dimethylnaphthalene	581-42-0	78.6 ± 1.8	3	104.6	90.4	94.1	83.0	82.8	82.6
2,7-Dimethylnaphthalene	582-16-1	79.5 ± 0.6	3	104.6	90.4	94.1	83.0	82.7	82.4
1,2,3-Trimethylnaphthalene	879-12-9			91.0	62.8	89.53	72.9	63.6	63.2
1,2,4-Trimethylnaphthalene	2717-42-2			88.0	65.0	84.6	68.0	58.6	58.3
1,2,5-Trimethylnaphthalene	641-91-8			87.9	65.0	84.6	68.0	58.5	58.2
1,2,6-Trimethylnaphthalene	3031-05-8			83.0	58.5	80.0	63.4	57.0	56.7
1,2,7-Trimethylnaphthalene	486-34-0			83.9	58.6	80.1	63.5	57.0	56.6
1,2,8-Trimethylnaphthalene	3876-97-9			110.3	83.1	115.2	98.6	86.2	85.8
1,6,7-Trimethylnaphthalene	2245-38-7			80.2	60.9	72.7	56.0	50.1	49.7
2,3,6-Trimethylnaphthalene	829-26-5			75.8	55.2	69.0	52.4	49.5	49.1
1,3,8-Trimethylnaphthalene	17057-91-9			101.1	76.2	101.8	85.2	76.2	75.9
1,4,5-Trimethylnaphthalene	2131-41-1			107.6	84.3	109.3	92.7	80.7	80.3
1,3,5-Trimethylnaphthalene	2131-39-7			81.8	63.1	74.7	58.1	51.0	50.7
1,3,6-Trimethylnaphthalene	3031-08-1			76.9	56.6	69.7	53.1	49.7	49.4
1,3,7-Trimethylnaphthalene	2131-38-6			77.7	57.5	70.0	53.4	47.6	47.2
1,4,6-Trimethylnaphthalene	2131-42-2			82.2	63.7	74.5	57.9	49.9	49.5
1,2,4,5-Tetramethylnaphthalene	99486-62-1			82.0	47.1	90.62	68.5	53.1	52.6
1,2,7,8-Tetramethylnaphthalene	99486-64-3			85.0	51.1	99.48	77.3	60.7	60.2
1,2,6,7-Tetramethylnaphthalene	99486-63-2			54.3	29.4	54.7	32.6	23.5	23.0
1,2,4,8-Tetramethylnaphthalene	66577-22-8			84.3	52.2	94.01	71.9	55.4	54.9
1,2,4,6-Tetramethylnaphthalene	66577-21-7			56.5	25.6	56.36	34.2	23.2	22.7
1,2,3,6-Tetramethylnaphthalene	66577-20-6			58.7	23.3	61.26	39.1	29.7	29.2
1,2,6,8-Tetramethylnaphthalene	66577-00-2			78.1	43.6	88.04	65.9	51.5	51.0
1,2,3,7-Tetramethylnaphthalene	51958-56-6			59.6	23.3	61.73	39.6	29.7	29.2
1,2,3,4-Tetramethylnaphthalene	3031-15-0			75.9	31.8	84.86	62.7	48.5	48.0
1,2,5,7-Tetramethylnaphthalene	38157-33-4			56.7	25.7	56.43	34.3	24.3	23.8
1,3,5,8-Tetramethylnaphthalene	14558-12-4			75.5	44.9	80.56	58.4	45.8	45.3
1,4,6,7-Tetramethylnaphthalene	13764-18-6			55.8	27.7	49.21	27.1	17.8	17.3
1,2,3,5-Tetramethylnaphthalene	13093-32-8			63.6	29.6	66.34	44.2	31.0	30.5
1,3,6,7-Tetramethylnaphthalene	7435-50-9			48.1	21.5	44.77	22.6	16.1	15.6
1,3,5,7-Tetramethylnaphthalene	7383-94-0			50.5	23.8	46.77	24.6	17.3	16.8
1,2,5,8-Tetramethylnaphthalene	3031-16-1			84.1	52.0	93.92	71.8	55.5	55.0
1,2,5,6-Tetramethylnaphthalene	2131-43-3			62.0	39.6	66.15	44.0	31.4	30.9
2,3,6,7-Tetramethylnaphthalene	1134-40-3			47.0	20.1	44.17	22.0	16.3	15.8
1,2,3,8-Tetramethylnaphthalene	1079-07-8			84.7	49.2	97.1	75.0	57.7	57.2
1,4,5,8-Tetramethylnaphthalene	2717-39-7			104.6	70.7	119.61	97.5	80.1	79.6
1,2,4,7-Tetramethylnaphthalene	16020-17-0			56.5	32.4	56.33	34.2	23.3	22.8
1,3,6,8-Tetramethylnaphthalene	14558-14-6			68.9	36.7	72.63	50.5	41.5	41.0

<sup>a</sup> These values calculated using the isodesmic equation, Eq. (1).<sup>b</sup> These values calculated using the homodesmotic equation, Eq. (2).

to calculate the energies of the homologous series of methyl substituted benzene isomers and compared those results with the experimental values (Table 1). There was good agreement between the experimental and computational results. However, these results show that as the number of atoms in a molecule increases, the accuracy of the simpler methods (AM1, PM3, B3PW91 isodesmic, B3PW91 homodesmotic) decreases sharply. The root-mean squared (RMS) deviation of these calculations from the experimental values are  $13.8 \text{ kJ mol}^{-1}$ ,  $11.7 \text{ kJ mol}^{-1}$ ,  $24.3 \text{ kJ mol}^{-1}$ , and  $7.5 \text{ kJ mol}^{-1}$ , respectively, while the G3MP2 method has a RMS value of  $1.2 \text{ kJ mol}^{-1}$  (isodesmic) and  $1.3 \text{ kJ mol}^{-1}$  (homodesmotic).

After validating the method, we calculated the enthalpies of formation of the homologous series of methyl substituted naphthalene isomers (Table 2) using the same computational methods

and the homodesmotic and isodesmic reactions described by Eqs. (1) and (2).

### 3. Discussion

This work compiles the calculated and measured enthalpy of formation data for all of the methyl substituted naphthalenes and benzenes into a single source. We have calculated the enthalpies of formation using the Gaussian 03 modeling programs and the AM1, PM3, B3PW91, and G3MP2 methods. For the B3PW91 and G3MP2 methods, the enthalpies of formation were calculated using both the isodesmic and homodesmotic reactions. The results from the methyl substituted naphthalene calculations are presented in Tables 2a and 2b.

**Table 2b**  
Methyl substituted naphthalenes. Experimental and calculated  $\Delta H_f^\circ_{298}$  values in  $\text{kJ mol}^{-1}$ .

Name	CAS	Expt.	Reference	AM1	PM3	B3PW91 6-31++G(d,p)		G3MP2	
						iso <sup>a</sup>	homo <sup>b</sup>	iso <sup>a</sup>	homo <sup>b</sup>
1,2,3,4,6-Pentamethylnaphthalene	56908-79-3			43.7	-6.8	57.0	29.4	14.9	14.3
1,2,3,4,5-Pentamethylnaphthalene	56908-78-2			71.3	21.0	95.2	67.5	45.3	44.7
1,2,3,5,7-Pentamethylnaphthalene	209978-64-3			32.4	-9.8	38.4	10.7	-2.9	-3.5
1,2,3,6,7-Pentamethylnaphthalene	209978-63-2			30.0	-11.9	36.8	9.1	-3.6	-4.2
1,2,3,5,6-Pentamethylnaphthalene	209978-62-1			37.7	-8.0	48.3	20.6	4.1	3.5
1,2,4,6,7-Pentamethylnaphthalene	171083-67-3			30.1	-9.7	35.3	7.6	-9.1	-9.8
1,2,4,6,8-Pentamethylnaphthalene	92556-54-2			52.1	12.8	65.2	37.5	18.5	17.9
1,2,3,5,8-Pentamethylnaphthalene	92556-53-1			58.4	18.2	75.3	47.6	26.9	26.3
1,2,4,5,6-Pentamethylnaphthalene	68844-46-2			58.2	14.9	75.0	47.3	28.1	27.4
1,2,4,5,8-Pentamethylnaphthalene	2928-64-5			79.2	38.5	105.1	77.4	54.8	54.1
1,2,3,6,8-Pentamethylnaphthalene	66577-20-6			52.5	9.7	68.3	40.6	24.9	24.3
1,2,3,7,8-Pentamethylnaphthalene	1164113-50-1			59.0	17.1	79.2	51.5	31.6	30.9
1,2,4,5,7-Pentamethylnaphthalene	1103580-53-5			49.9	7.8	61.8	34.1	18.2	17.6
1,2,4,7,8-Pentamethylnaphthalene	1164113-56-7			58.6	20.1	77.0	49.3	29.3	28.6
1,2,3,4,5,6-Hexamethylnaphthalene	56908-83-9			45.1	-10.3	76.2	43.0	16.9	16.1
1,2,3,4,5,7-Hexamethylnaphthalene	56908-77-1			39.2	-18.3	67.0	33.8	10.9	10.1
1,2,3,4,6,7-Hexamethylnaphthalene	17384-76-8			14.9	-42.9	31.9	-1.3	-18.5	-19.2
1,2,3,5,6,7-Hexamethylnaphthalene	51958-57-7			13.5	-43.4	29.9	-3.3	-23.0	-23.7
1,2,3,5,6,8-Hexamethylnaphthalene	872010-01-0			32.6	-17.4	57.3	24.1	1.1	0.4
1,2,3,5,7,8-Hexamethylnaphthalene	1164113-71-6			32.6	-14.0	57.3	24.0	-0.2	-0.9
1,2,3,6,7,8-Hexamethylnaphthalene	1164113-72-7			33.0	-15.1	59.4	26.2	2.4	1.6
1,2,3,4,5,8-Hexamethylnaphthalene	36230-30-5			65.4	15.9	105.7	72.5	41.6	40.8
1,2,4,5,6,8-Hexamethylnaphthalene	1164113-75-0			53.7	5.6	87.7	54.5	27.9	27.1
1,2,4,5,7,8-Hexamethylnaphthalene	1164113-78-3			52.5	5.5	84.9	51.7	24.7	24.0
1,2,3,4,5,6,8-Heptamethylnaphthalene	259743-98-1			38.4	-19.2	85.2	46.5	11.4	10.5
1,2,3,4,5,6,7-Heptamethylnaphthalene	56908-82-8			19.2	-44.3	57.6	18.8	-12.4	-13.3
1,2,3,4,5,6,7,8-Octamethylnaphthalene	18623-61-5			22.4	-39.1	81.4	37.1	-5.8	-6.8

<sup>a</sup> These values calculated using the isodesmic equation, Eq. (1).

<sup>b</sup> These values calculated using the homodesmotic equation, Eq. (2).

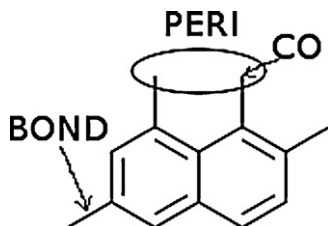
We compared the accuracy of the methyl substituted naphthalene results, obtained from the isodesmic and homodesmotic reactions for both the G3MP2 and B3PW91 calculations, to the experimental values. Using the G3MP2 calculated values, the enthalpy of formation determined by the isodesmic and homodesmotic reactions are greater than the experimental enthalpy of formation by an average of  $3.4 \text{ kJ mol}^{-1}$  and  $3.3 \text{ kJ mol}^{-1}$ , respectively. For the B3PW91 calculated values, the enthalpy of formation determined by the isodesmic and homodesmotic reactions are greater than the experimental enthalpy of formation by an average of  $14.5 \text{ kJ mol}^{-1}$  and  $6.0 \text{ kJ mol}^{-1}$ , respectively. From these results and those of the methyl substituted benzenes it is clear that the homodesmotic reaction provides a more accurate method of calculating the enthalpy of formation when using lower levels of theory.

The enthalpies of formation values calculated by the AM1 and PM3 methods are greater than the experimental values of the naphthalene series by an average of  $24.7 \text{ kJ mol}^{-1}$  and  $14.9 \text{ kJ mol}^{-1}$ , respectively. When compared to the homodesmotic G3MP2 values, the values obtained by these methods are greater by an average of  $29.3 \text{ kJ mol}^{-1}$  and  $13.2 \text{ kJ mol}^{-1}$ .

It is well known that energies computed by DFT functionals are flawed by systematic errors, which can become considerable for larger molecules [19]. This is the exact trend we found when we

compared the homodesmotic B3PW91 results to the homodesmotic G3MP2 results. The B3PW91 results are greater than the G3MP2 results by an average of  $15.7 \text{ kJ mol}^{-1}$ .

While the G3MP2 results are the most accurate, they are also the most computationally expensive. In the pharmaceutical industry, this expense is prohibitive for screening the large numbers of compounds in their drug libraries. So, these companies and other industrial players turn to other methods to determine the properties of interest. One of these methods is group additivity. As described previously, the group additivity method determines the number and types of groups in a molecule, looks up the values assigned to each group, and sums these values together [6]. This method is fast, simple, and accurate; however, its accuracy is low for complex molecules because values are assigned to each group, not to the interactions between groups. The attempt to overcome this limitation by assigning values to the group interactions was the driving force for the Whiteside and Carreria paper [5]. While that work was successful for the compounds studied, it was limited by the lack of experimental data available to determine the group interactions.



**Fig. 1.** Methyl interactions in benzene or naphthalene.

**Table 3**

Group additivity parameters, in  $\text{kJ mol}^{-1}$ , for methyl substituted benzene and naphthalene compounds.

Name	Description	Value (G3MP2)	Value (B3PW91)
Methane base value		-74.9	-74.9
Benzene base value		82.9	82.9
Naphthalene base value		150.6	150.6
BOND	$\text{CH}_3\text{-CH}_2$ bond energy	41.4	43.1
CO	Constrained ortho group	6.9	9.0
PERI	Peri interaction	15.0	18.1

**Table 4a**Group additivity results for the methyl substituted benzenes. All  $\Delta H_f^{\circ 298}$  values in  $\text{kJ mol}^{-1}$ .

Name	$\Delta H_f^{\circ 298}$ calc (G3MP2)	Methyl	Nap	BOND	CO	$\Delta H_f^{\circ 298}$ calc (GA)	$\Delta (\Delta H_f^{\circ 298})$
Benzene	82.9	0	1	0	0	82.9	0.0
1-Methylbenzene	50.2	1	1	1	0	48.7	1.5
1,2-Dimethylbenzene	16.8	2	1	2	0	16.0	0.8
1,3-Dimethyl	17.7	2	1	2	0	14.5	3.2
1,4-Dimethylbenzene	18.3	2	1	2	0	14.5	3.7
1,2,3-Trimethylbenzene	-10.9	3	1	3	1	-10.6	-0.3
1,2,4-Trimethylbenzene	-15.3	3	1	3	0	-18.2	2.9
1,3,5-Trimethylbenzene	-14.8	3	1	3	0	-19.7	4.9
1,2,3,4-Tetramethylbenzene	-38.2	4	1	4	2	-37.2	-1.1
1,2,3,5-Tetramethylbenzene	-42.8	4	1	4	1	-4.8	1.9
1,2,4,5-Tetramethylbenzene	-48.3	4	1	4	0	-50.9	2.7
1,2,3,4,5-Pentamethylbenzene	-65.0	5	1	5	3	-63.7	-1.2
1,2,3,4,5,6-Hexamethylbenzene	-77.6	6	1	6	6	-76.5	-1.1

Here, we have calculated the group additivity interaction parameters for methyl substituted benzene and naphthalene compounds. While simple for “straight-chain” aromatics (benzene, naphthalene, anthracene, etc.), other aromatic compounds (phenanthrene, pyrene, etc.) have multiple interactions and enu-

merating them consistently and elucidating their values becomes exponentially more difficult. For this reason, it is an open question of whether calculating the compounds values using a high-level of theory or developing a comprehensive group additivity method is the more efficient and accurate method. The developed group

**Table 4b**Group additivity results for the 0-4 methyl substituted naphthalenes. All  $\Delta H_f^{\circ 298}$  values in  $\text{kJ mol}^{-1}$ .

Name	$\Delta H_f^{\circ 298}$ calc (G3MP2)	Methyl	Nap	BOND	CO	PERI	$\Delta H_f^{\circ 298}$ calc (GA)	$\Delta (\Delta H_f^{\circ 298})$
Naphthalene	150.6	0	1	0	0	0	150.6	0.0
1-Methylnaphthalene	117	1	1	1	0	0	117.0	0.0
2-Methylnaphthalene	118.3	1	1	1	0	0	118.5	-0.2
1,2-Dimethylnaphthalene	84.5	2	1	2	1	0	84.8	-0.3
1,3-Dimethylnaphthalene	83.6	2	1	2	0	0	83.3	0.3
1,4-Dimethylnaphthalene	83.8	2	1	2	0	0	83.3	0.5
1,5-Dimethylnaphthalene	84.1	2	1	2	0	0	84.7	-0.6
1,6-Dimethylnaphthalene	86.5	2	1	2	0	0	86.4	0.1
1,7-Dimethylnaphthalene	111.9	2	1	2	0	1	114.9	-3.0
1,8-Dimethylnaphthalene	91.9	2	1	2	0	0	92.5	-0.6
2,3-Dimethylnaphthalene	86.6	2	1	2	0	0	86.4	0.2
2,6-Dimethylnaphthalene	84.8	2	1	2	0	0	84.8	0.0
2,7-Dimethylnaphthalene	84.7	2	1	2	0	0	84.8	-0.1
1,2,3-Trimethylnaphthalene	65	3	1	3	2	0	66.4	-1.4
1,2,4-Trimethylnaphthalene	60	3	1	3	1	0	60.3	-0.3
1,2,5-Trimethylnaphthalene	59.9	3	1	3	1	0	60.3	-0.4
1,2,6-Trimethylnaphthalene	58.45	3	1	3	1	0	58.8	-0.4
1,2,7-Trimethylnaphthalene	58.36	3	1	3	1	0	58.8	-0.5
1,2,8-Trimethylnaphthalene	87.56	3	1	3	1	1	88.8	-1.3
1,6,7-Trimethylnaphthalene	51.49	3	1	3	0	0	52.6	-1.1
2,3,6-Trimethylnaphthalene	50.87	3	1	3	0	0	51.1	-0.2
1,3,8-Trimethylnaphthalene	77.64	3	1	3	0	1	81.2	-3.6
1,4,5-Trimethylnaphthalene	82.1	3	1	3	0	1	82.7	-0.6
1,3,5-Trimethylnaphthalene	52.44	3	1	3	0	0	52.7	-0.3
1,3,6-Trimethylnaphthalene	51.15	3	1	3	0	0	51.2	-0.1
1,3,7-Trimethylnaphthalene	49.01	3	1	3	0	0	51.2	-2.2
1,4,6-Trimethylnaphthalene	51.27	3	1	3	0	0	52.7	-1.5
1,2,4,5-Tetramethylnaphthalene	55.03	4	1	4	1	1	56.7	-1.7
1,2,7,8-Tetramethylnaphthalene	62.57	4	1	4	2	1	62.8	-0.2
1,2,6,7-Tetramethylnaphthalene	25.39	4	1	4	1	0	26.6	-1.2
1,2,4,8-Tetramethylnaphthalene	57.33	4	1	4	1	1	56.7	0.6
1,2,4,6-Tetramethylnaphthalene	25.03	4	1	4	1	0	26.7	-1.7
1,2,3,6-Tetramethylnaphthalene	31.58	4	1	4	2	0	32.8	-1.2
1,2,6,8-Tetramethylnaphthalene	53.39	4	1	4	1	1	55.2	-1.8
1,2,3,7-Tetramethylnaphthalene	31.6	4	1	4	2	0	32.8	-1.2
1,2,3,4-Tetramethylnaphthalene	50.41	4	1	4	4	0	48.1	2.3
1,2,5,7-Tetramethylnaphthalene	26.19	4	1	4	1	0	26.7	-0.5
1,3,5,8-Tetramethylnaphthalene	47.66	4	1	4	0	1	49.1	-1.4
1,4,6,7-Tetramethylnaphthalene	19.65	4	1	4	0	0	20.5	-0.9
1,2,3,5-Tetramethylnaphthalene	51.27	4	1	4	2	0	34.3	17.0
1,3,6,7-Tetramethylnaphthalene	18.02	4	1	4	0	0	19.0	-1.0
1,3,5,7-Tetramethylnaphthalene	19.13	4	1	4	0	0	19.1	0.0
1,2,5,8-Tetramethylnaphthalene	57.38	4	1	4	1	1	56.7	0.7
1,2,5,6-Tetramethylnaphthalene	33.3	4	1	4	2	0	34.3	-1.0
2,3,6,7-Tetramethylnaphthalene	18.17	4	1	4	0	0	18.9	-0.7
1,2,3,8-Tetramethylnaphthalene	59.55	4	1	4	2	1	62.8	-3.2
1,4,5,8-Tetramethylnaphthalene	82	4	1	4	0	2	79.1	2.9
1,2,4,7-Tetramethylnaphthalene	25.15	4	1	4	1	0	26.7	-1.6
1,3,6,8-Tetramethylnaphthalene	43.35	4	1	4	0	1	47.6	-4.2

**Table 4c**  
Group additivity results for the 5–8 methyl substituted naphthalenes. All  $\Delta H_f^{\circ 298}$  values in  $\text{kJ mol}^{-1}$ .

Name	$\Delta H_f^{\circ 298}$ calc (G3MP2)	Methyl	Nap	BOND	CO	PERI	$\Delta H_f^{\circ 298}$ calc (GA)	$\Delta (\Delta H_f^{\circ 298})$
1,2,3,4,6-Pentamethylnaphthalene	17.27	5	1	5	4	0	14.5	2.8
1,2,3,4,5-Pentamethylnaphthalene	47.64	5	1	5	4	1	44.5	3.2
1,2,3,5,7-Pentamethylnaphthalene	-0.53	5	1	5	2	0	0.7	-1.2
1,2,3,6,7-Pentamethylnaphthalene	-1.27	5	1	5	2	0	0.6	-1.8
1,2,3,5,6-Pentamethylnaphthalene	6.46	5	1	5	3	0	8.3	-1.8
1,2,4,6,7-Pentamethylnaphthalene	-6.79	5	1	5	1	0	-5.5	-1.3
1,2,4,6,8-Pentamethylnaphthalene	20.83	5	1	5	1	1	23.1	-2.2
1,2,3,5,8-Pentamethylnaphthalene	29.24	5	1	5	2	1	33.8	-4.5
1,2,4,5,6-Pentamethylnaphthalene	30.42	5	1	5	2	1	23.0	7.5
1,2,4,5,8-Pentamethylnaphthalene	57.12	5	1	5	1	2	53.1	4.1
1,2,3,6,8-Pentamethylnaphthalene	27.24	5	1	5	2	1	29.1	-1.9
1,2,3,7,8-Pentamethylnaphthalene	33.9	5	1	5	3	1	36.7	-2.8
1,2,4,5,7-Pentamethylnaphthalene	20.59	5	1	5	1	1	23.1	-2.5
1,2,4,7,8-Pentamethylnaphthalene	31.61	5	1	5	2	1	30.7	0.9
1,2,3,4,5,6-Hexamethylnaphthalene	19.71	6	1	6	5	1	18.4	1.3
1,2,3,4,5,7-Hexamethylnaphthalene	13.68	6	1	6	4	1	10.8	2.9
1,2,3,4,6,7-Hexamethylnaphthalene	-15.67	6	1	6	4	0	-17.8	2.1
1,2,3,5,6,7-Hexamethylnaphthalene	-20.16	6	1	6	4	0	-17.8	-2.4
1,2,3,5,6,8-Hexamethylnaphthalene	3.92	6	1	6	3	1	4.6	-0.7
1,2,3,5,7,8-Hexamethylnaphthalene	2.64	6	1	6	3	1	4.6	-2.0
1,2,3,6,7,8-Hexamethylnaphthalene	5.21	6	1	6	4	1	10.7	-5.5
1,2,3,4,5,8-Hexamethylnaphthalene	44.38	6	1	6	4	2	40.8	3.6
1,2,4,5,6,8-Hexamethylnaphthalene	30.68	6	1	6	2	2	27.0	3.7
1,2,4,5,7,8-Hexamethylnaphthalene	27.55	6	1	6	2	2	27.0	0.5
1,2,3,4,5,6,8-Heptamethylnaphthalene	14.64	7	1	7	5	2	14.8	-0.1
1,2,3,4,5,6,7-Heptamethylnaphthalene	-9.1	7	1	7	6	1	-15.3	6.2
1,2,3,4,5,6,7,8-Octamethylnaphthalene	-2.07	8	1	8	8	2	2.5	-4.6

additivity method uses the base value of the aromatic compound (benzene or naphthalene) and three parameters: the  $\text{CH}_3\text{--CH}_2$  bond (BOND), constrained “ortho” (CO), and the “peri” (PERI) interactions. These interactions are per bonding group, in this case the methyl group, and are depicted in Fig. 1. These parameter values were determined by enumerating the groups and group interactions in each molecule and then using a least-squares fit to minimize the difference between the calculated (G3MP2 and B3PW91) values and the values obtained by using the group additivity interaction parameters. This is the same method originally outlined by Benson and further refined by Whiteside, Joback, and Gronert, among others [5,6,20,21]. The values of these parameters are presented in Table 3. It is worth noting that the average difference between the parameter values obtained by G3MP2 versus B3PW91 is  $2.3 \text{ kJ mol}^{-1}$ . This implies that while the parameters obtained by the G3MP2 values are the most accurate, the cheaper DFT method may also be used to determine these parameters values, with only a small loss in accuracy. However, the reader should be cautioned that since the parameters are additive, as the number of times each is used increases, the difference between the parameters will increase as well.

The enumeration and calculation of the substituted benzene and naphthalene compounds are presented in Tables 4a–4c using the G3MP2 calculated values. The group additivity method worked well for these compounds, with the twelve substituted benzene compounds having a RMS value of  $1.8 \text{ kJ mol}^{-1}$  and the seventy-five substituted naphthalene compounds having a RMS value of  $2.1 \text{ kJ mol}^{-1}$  when compared to the G3MP2 values.

#### 4. Conclusions

This work calculated the enthalpy of formation for all of the methyl substituted naphthalene compounds using multiple levels of theory. The highest level calculation (G3MP2) agreed well with all of the experimentally determined values, although it is computationally expensive. The differences between calculated values vary greatly between the different computational methods.

A group-additivity model was developed by determining the intra-molecular interactions and, based on the results of the G3MP2 and B3PW91 calculations, assigned values. These values were compared and found to differ by  $2.3 \text{ kJ mol}^{-1}$ . This implies that while DFT calculations on a single molecule may be inaccurate, by coupling these calculations with a group additivity method, and using a large collection of molecules, these inaccuracies may be mitigated and useful results obtained. The group additivity method produces acceptable results; however, it is an inflexible model, and without the appropriate experimental (or calculated) values, it cannot be extensively or accurately developed. For these reasons, it may be more appropriate to carry out the high-level calculations versus developing a group-additivity model for complex molecules.

In future work, we plan to continue this series of calculations to methyl substituted phenanthrene, pyrene, and other aromatic compounds. This will allow us to determine other interactions and verify that the interactions are consistent between types of molecules using the group-additivity model as well as compare the calculated results to the experimental values.

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